

# Analysis of RSA Cryptosystem to Secure Messages in Vehicular Adhoc Network

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**Abstract:** Due to increasing rate of accidents as per World Health Organisation, it is required to provide safety in Vehicals. Even if provided safety features in vehicals such as airbags, safety belts , still rate of accidents ratio not reduced. Most of accidents occurs at intersection points. If preincident information about incident received then motorist may take decision along the path . But , difficulty is that if such messages are not secured among vehicals in network then attacker may broadcast wrong information in network for personal benefits or for just fun which may be life threatening to other users in network as other users decisions in network depends only on messages received.

Hence, Security of such Network is important. In this paper, tried to analyse the performance of RSA Cryptographic algorithms in terms of Delay. i. e. time required to generate keys , time required for signature Generation & Signature Verification . Finally conclude whether RSA cryptosystem is suitable for Vehicular adhoc network Communication or Not.

**Keywords:** Public Key Management system, VANET .

## 1. Introduction

VANET is Vehicular Adhoc Network in which each vehicle will act as node, which will transmit as well as receive message. In VANET, Roadside units also acts as Transmitter-Receiver Section. Base Station will broadcast messages in its covering Range of Vehicles Network. VANET main aim is to provide safety related messages such as traffic information , internet services shown in figure 1.

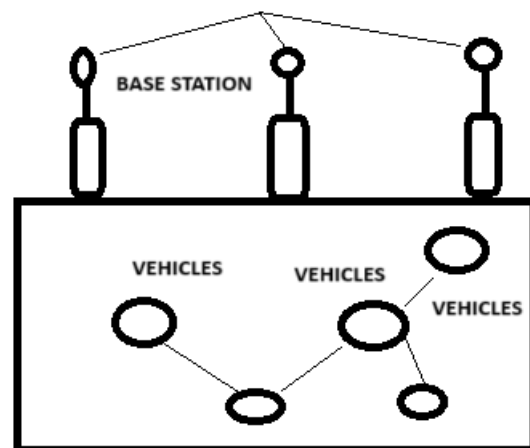


Fig 1 Vehicle Infrastructure

Safety related messages which will be broadcast in network must be secured. User decision totally depends only on received messages. If wrong information received by user which will be life threatening to user or to other nodes in network . Hence Security of such system is important. With the help of Symmetric or asymmetric key cryptosystem , security of safety related message can be provide.

## Issues while Providing Security in VANET

1. As per Dedicated Short Range Communication, Each message must be process in  $1 \times 10^{-9}$  seconds as DSRC operated at 5.9 GHZ frequency
2. In Symmetric Key Cryptosystem , Sender and receiver use same key to encrypt as well as to decrypt messages.

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If this key track by attacker then unauthorized user of system may take control of system and then may broadcast wrong information in network.

3. Routing Protocol , Speed of Vehicles , Broadcasting Range, availability of network range, are also an issues in Vehicular Adhoc Network.

From above issues, it is conclude that the VANET is vast area of research in which need to work on each aspect like routing protocol, Range of Node and also cryptosystem to secure messages in network.

In this Paper, Cryptographic Algorithm is taken as challenging task and with the help of this algorithm , tried to provide Solution.

## 2. Objectives

To Make Key management system flexible

To increase the throughput of the system

To reduce overheads

These objectives can be achieved by using appropriate algorithms and routing protocols

## 3. Related Work

After key management techniques have been employed there is considerable improvement in the data communication between the nodes [1]

The related protocol and the proposed security architecture has shown to what extent and how it protects privacy[2]

Both security concerns and the requirement of the potential VANET application are taken into account in a proposed secured and application oriented network design framework [3].

Presented Temporary Anonymous Certified Keys (tacks) as an efficient way to fulfill the Security and Privacy Properties Necessary for Key Management in Vehicular Ad Hoc Networks (vanets). [4]

Proposed a Practical Ways of Defending Against Sybil Attack in a VANET Environment, Which Require Neither a Dedicated Vehicular Public Key Infrastructure for Individual Vehicles, nor Additional Setup, but only Basic Roadside units. [5]

For defending against sybil attack in a VANET environment practical ways are proposed which neither requires an additional setup nor dedicated vehicular public key infrastructure for individual vehicles, but only basic roadside units.

Proposed an Applicable Method for Securing Safety Message and Solve Problems Facing During Implementation [6]

Applicable methods are proposed for securing safety message and solve problems facing during implementation.

### Role of Routing Protocol in VANET

If node A wish to send Message to Node B then initially Node A will broadcast “Hello” kind of message in network .This “Hello” message contains Node ID’s. So that , other nodes in network can get idea about their surrounding nodes in network . After reception of this message any node in network can establish communication with other nodes in network. Node A will send Request to Node B as node A wish to send Message to Node B. This request message will contains node id, sequence number , hope count etc. After received, request from Node A , node B will check whether request is for himself or for other nodes based on parameters mentioned in request message. After received request , if node B wish to establish communication with node A then node B will send reply to Node A. After received Reply from Node B , Node A will start to send messages to node B in network as shown in figure 2.

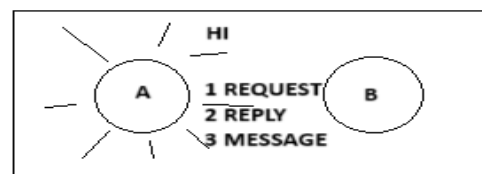


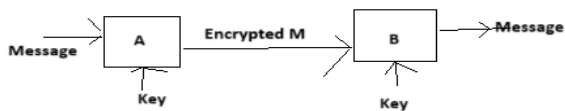
Fig 2 Communication Establishment in Adhoc Network

If Attacker is listening their communication then may easily hack such system that I am active member of network and have shortest path and fresh route to destination.

With the help of Cryptosystem , tried to provide solution. How Symmetric and Assymetric Key Cryptographic algorithms will works that have explained with the help of following figures.

### Symmetric Key Cryptography Algorithm :

If Node A wish to send message to Node B in network. First Node A will Encrypt Hello message with the help of Symmetric Key Cryptographic based Algorithm by using Secrete key. Node B will decrypt this Hello message using the same secrete key . Node B will confirm that the message received from authorized source . Only authorized nodes in network will have this secured key provided by key management system . Hence , only authorized nodes in network can read messages. But, Difficulty in this mechanism is that Attacker may easily get this secrete key which have explained with figure 3 .



**Fig 3.** Assymmetric Key Algorithm

After received number of messages , attacker can use currently available Symmetric Cryptographic based algorithms like AES or DES and will try to apply different keys to decrypt message and at which key Attacker will get meaningful message, attacker will get that secrete key . once attacker get the key then attacker can easily control the system.

#### Solution to Existing System

With the help of Asymmetric Key Cryptography Algorithm ,have tried to provide solution. Here, have considered Asymmetric Key Cryptography Algorithm i .e. RSA Cryptographic Algorithm. How RSA cryptosystem will work in vehicular adhoc network that have explained.

If Node A wish to send messages to node B then node A will first broadcast hello message in network by encrypting with the help of Private key provided to node A. After received hello message , node B will decrypt the message with the help of public key available to node B. Only authorized nodes in network will have these two keys Public key and Private Key. By using Private Key , any node in network can encrypt messages and by using Public Key any nodes in network can decrypt messages. Using Assymmetric key Cryptographic Algorithm, its becomes difficult for attacker to get that private key as each nodes in network will have different private keys .Hence, in this paper have studied Assymmetric key Cryptographic Algorithm i.e. RSA Algorithm and have analyzed its performance in terms of time require for Key Generation, time require for Signature Generation and Verification.

#### RSA Algorithm

RSA ( Rivest- Shamir-Adleman ) is an algorithm used to encrypt and decrypt messages. This Algorithm developed by three authors Rivest- Shamir-Adleman . That's why name of this algorithm is RSA. It is Asymmetric Cryptographic algorithm. In Asymmetric Cryptographic algorithm , we use public key and Private Key for encryption and decryption. So, both sender and receiver use private key and public key for encryption and decryption.

#### Encryption

$X = Y^e \text{ mod } n$  , where Y is original message and X is encrypted message. e is public key and n is product of two large prime numbers.

#### Decryption

$Y = X^d \text{ mod } n$  where Y is original message and X is encrypted message. e is public key and n is product of two large prime numbers.

#### Key Generation Algorithm in RSA Cryptosystem

First will select two large prime numbers a and b.

Secondly will calculate  $n = a \times b$  and then will calculate Eulers Function i.e.

$$\theta(n) = (a-1) \times (b-1)$$

$\times (b-1)$  .

In Next step, will choose a small number e, coprime to  $\theta(n)$  with  $\text{GCD}(\theta(n), e) = 1$  and  $1 < e < \theta(n)$ .

In last step , will find d , such that  $d \times e \text{ mod } \theta(n) = 1$ .

Let us see example for key Generation Algorithm.

First consider two prime numbers  $p=3$  ,  $q=5$

Then calculate  $n = p \times q$  therefore  $n = 3 \times 5 = 15$ .

$$\theta(n) = (p-1) \times (q-1)$$

$$\theta(n) = (3-1) \times (5-1)$$

$$\theta(n) = 8$$

Assume e such that  $\text{gcd}(e, \theta(n)) = 1$  and  $\text{GCD}(\theta(n), e) = 1$  and  $1 < e < \theta(n)$ .

$$\text{gcd}(3, 8) = 1$$

$$\text{gcd}(5, 8) = 1$$

$$\text{gcd}(7, 8) = 1$$

Out of these three , can select any one value which will satisfy the condition  $\text{GCD}(\theta(n), e) = 1$  and  $1 < e < \theta(n)$ .

Therefore  $e = 3$  is selected.

Now, in last step calculated d.

$$d \times e \text{ mod } \theta(n) = 1$$

$$d \times 3 \text{ mod } 8 = 1$$

Consider  $d = 3$

Therefore

$$3 \times 3 \text{ mod } 8 = 1$$

$$9 \text{ mod } 8 = 1$$

Therefore

$$d = 3$$

Now we have public key =  $\{e, n\} = \{3, 15\}$

Private Key =  $\{d, n\} = \{3, 15\}$

After Calculated Public and Private Key , tried to encrypt and decrypt messages.

Encryption

$$X = Y^e \text{ mod } n$$

Suppose  $Y = 8$  ( original message)

$$X = 8^3 \text{ mod } 15$$

$$X = 2 \text{ ( Encrypted Message )}$$

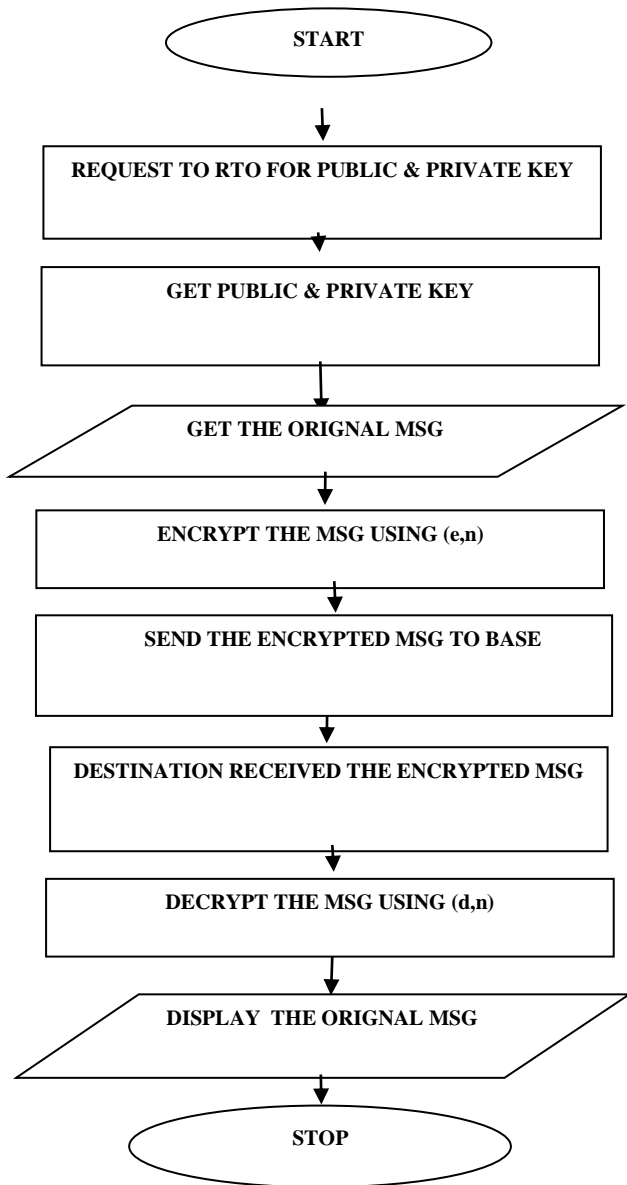
Decryption

$$Y = X^d \text{ mod } n$$

$$Y = 2^3 \text{ mod } 15$$

$$Y = 8 \text{ ( original Message )}$$

Use of RSA Cryptography Algorithm in VANET



#### 4. Result Analysis

In tabular form have represented some simulated results of RSA cryptography Algorithm for 1028 ,2048 and 4096 key length and Calculated time required for key generation , Signature generation and Signature Verification in  $10^{-9}$ seconds.

RSA 1024 Key Length

256R p4 2.8Ghz	1024
e	3
p	65380725939414761705852595117 33365414213441424081803846910 3932472260901245076191  89673752276652886189517360257 78723053906837161677149470805 02491432169079

q	69753739842748268836081639629 16622088282533527946320278776 1209494074221741831547  13626263564383759643597152476 42579709509100138110367838583 2861559015126527
phi	45605501479079607014653245970 98219011085876191320989817220 1195657985213077490239  11026314001067015676419267439 81730995741236168446416507087 6715133853325682640291  94228914561398898825190925937 99434021928489911301501622761 6260004360217380362767  41946923226645166862708469212 09071177090791613560843860847 94763028
m	12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210
Message encrypted	15273916995936178735607493695 00840113194490207488208458480 7451747363517947147238  37059996706625074978379753261 68015793532920611142322008288 4039814232738475614454  79816232671772886897269860379 48085009129877732178415953633 1298229675857580224043  06841908113837719807655685163 29006859291413238470160713273 8386243
signature generation time	0
decrypted msg	12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210

	12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210
signature verification time	47
Message signed	15273916995936178735607493695 00840113194490207488208458480 7451747363517947147238  37059996706625074978379753261 68015793532920611142322008288 4039814232738475614454  79816232671772886897269860379 48085009129877732178415953633 1298229675857580224043  06841908113837719807655685163 29006859291413238470160713273 8386243
sign time	47
verify time	0
Original message back, verified:	12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210
Message signed and encrypted,	14367793390310734815712597946 28738203321905078300220039460 0108636941711485518628  86710028936661006188019597423 79891551785970635730521918752 5788728433112277685336  82255467600709353550748484737 65886920538139017116511383488 9324853508230893824428  06067004339471877900751263242 74747628109009426909660571994 9918958058
sign and encrypt time	46

	12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210  12345678909876543210123456789 09876543210123456789098765432 1012345678909876543210
Original message back, verified and decrypted,	
decrypt and verify time	47

**Table 1** RSA 1024 256R P4 2.8Ghz

512 P4 2.8Ghz	1024
e	3
p	2117721817371107221459918814 8657408835062452971855259293 083427605161166018310137  8591532058161068643583008885 1141550252373703161486052104 509087534977339278061
q	3262368513127156944741311916 4836396711818489776216520691 905034150122521298405532  3206122018355210301554178849 2072841697332047144073358988 2821092828248583
phi	6908788976553919671346685560 3460357365438837401560752277 634297638986247206190455  2732762333253976150192503075 3522773791318642603151353113 211812197766417568044971  9107551866764256538735409214 3842065147429274280770076571 613100641889453808994064  5550824546617034993012566406 5075235389840103171010277500 706098710920
m	1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654

	321012345678909876543210
Message encrypted	4458359603445092537647615649 4624426287733131380544741909 185561010179581757406059  3886682778481004304563341102 6908315096929372010464213052 409902069112865150292483  7907327254455756389339047926 6960654429765914751423032438 340610742929940896857173  1157488768586715799279446786 5933659141566451302544780425 166670272440
signature generation time	0
decrypted msg	1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210
signature verification time	47
Message signed	4458359603445092537647615649 4624426287733131380544741909 185561010179581757406059  3886682778481004304563341102 6908315096929372010464213052 409902069112865150292483  7907327254455756389339047926 6960654429765914751423032438 340610742929940896857173  1157488768586715799279446786 5933659141566451302544780425 166670272440
sign time	47
verify time	0
Original message back, verified:	1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210

	1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210
Message signed and encrypted,	3930643630770736946201932804 7354545317536328165927637952 266151554828258152060365  9771746016216374185157508285 606795022205541871832454982 668165259271576736434268  1856130560534226424848158880 2669307409322562691171697994 766559261573315274855577  4652668554620235280909198749 5821272165766151666109692553 37788621950
sign and encrypt time	47
Original message back, verified and decrypted,	1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210  1234567890987654321012345678 9098765432101234567890987654 321012345678909876543210
decrypt and verify time	47

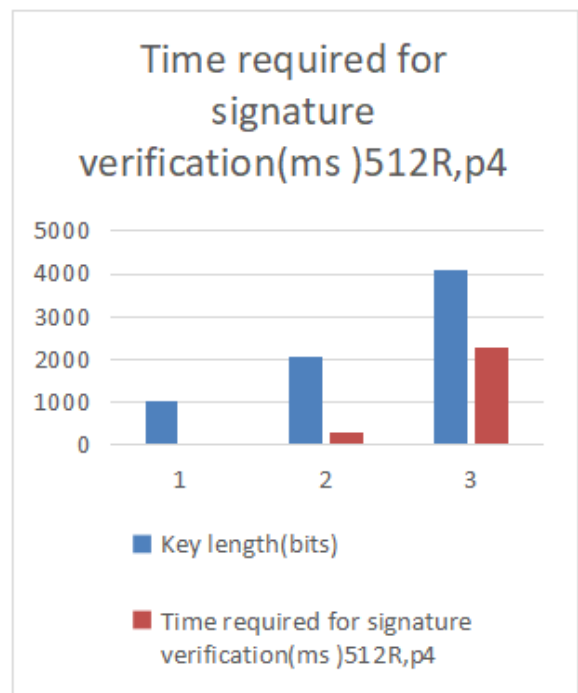
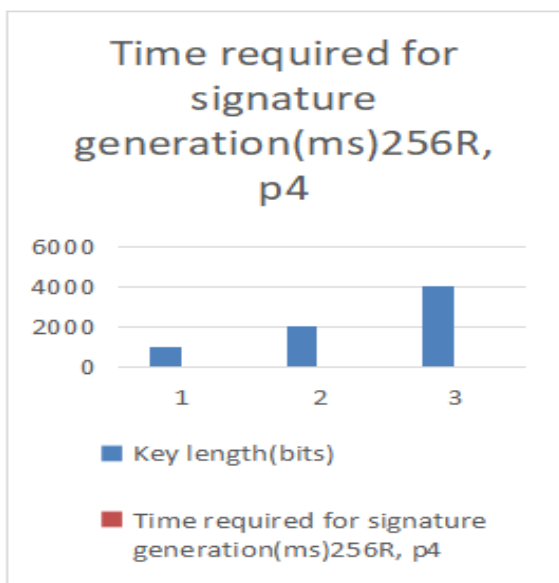
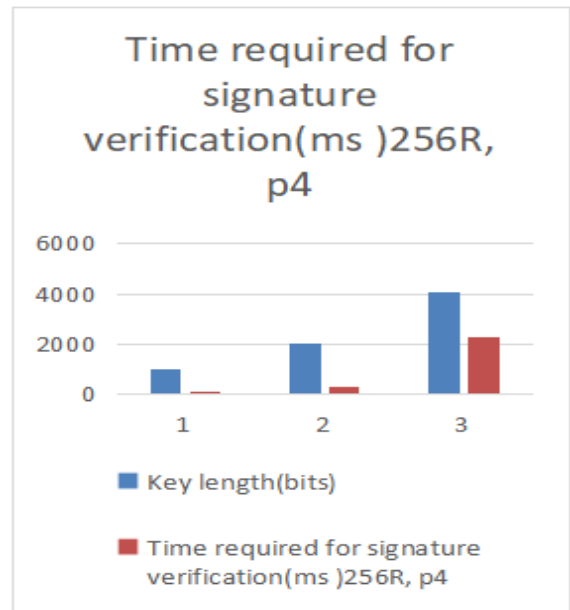
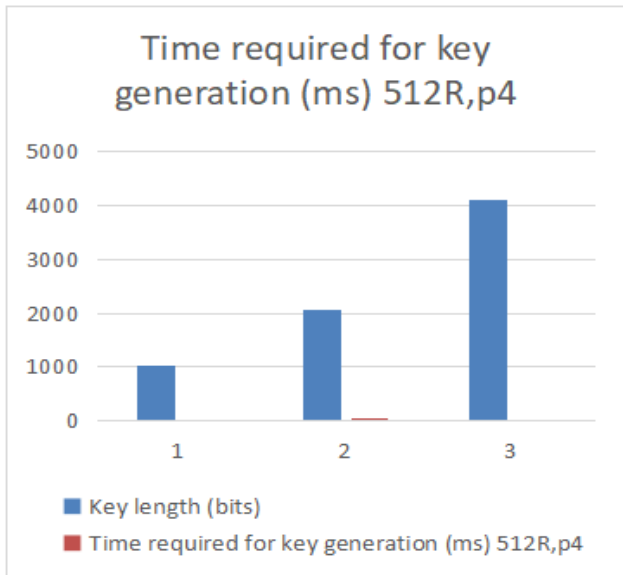
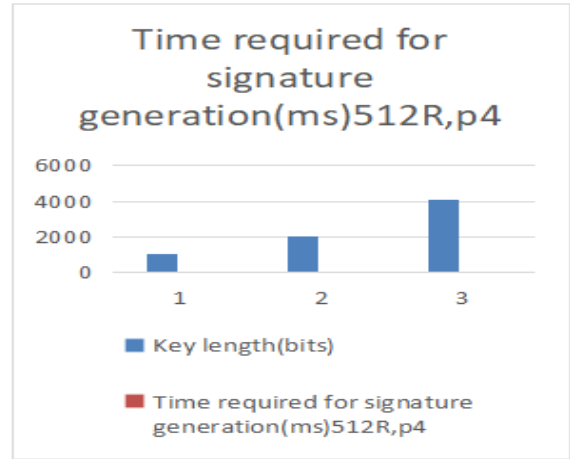
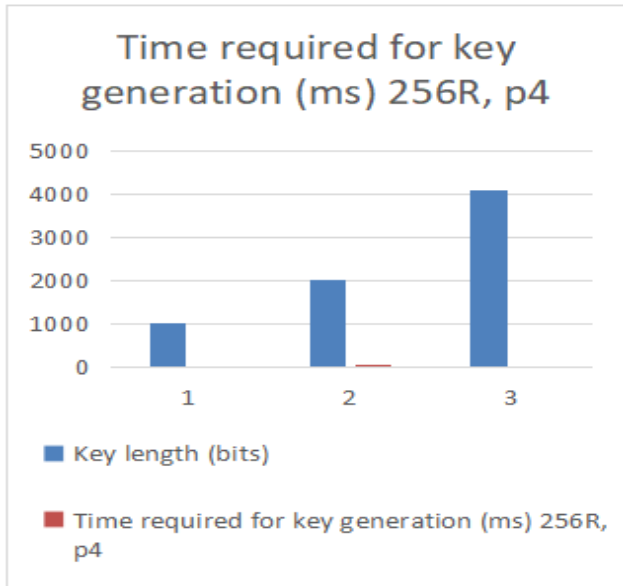
Table 2 RSA 1024 for 512R p4 2.8 Ghz

### Verification and Testing of Algorithms

TABLE 3 RSA ALGORITHM ANALYSIS

S.N	Key length (bits)	Time required for key generation (ms)		Time required for signature generation (ms)		Time required for signature verification (ms)	
		256R, p4	512R, p4	256R, p4	512R, p4	256R, p4	512R, p4
1	1024	0	32	0	0	47	47
2	2048	16	16	0	16	297	297
3	4096	47	32	0	0	2297	2297

**Graphical Analysis**



## 5. Conclusion

After implementing RSA algorithm, it has been observed that the time required for signature verification for 1024, 2048, 4096 bits respectively is on higher side

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