

# A Quantum Machine Learning Approach for Bridging the Gap Between Quantum and Classical Computing.

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**Abstract:** The relentless march of technological progress has ushered in an era where the computational boundaries between quantum and classical systems have become increasingly distinct. This research paper endeavors to traverse this schism, proposing innovative approaches aimed at bridging the gap between quantum and classical computing paradigms. The burgeoning capabilities of quantum computing hold promise for solving complex problems that elude classical systems; however, practical implementation faces formidable challenges. Through an in-depth exploration of the current landscape, this research identifies key gaps and issues impeding the seamless integration of quantum and classical computing. Our methodology involves a comprehensive review of existing approaches, coupled with theoretical modeling and empirical investigations where applicable. The results unveil novel insights into the convergence of quantum and classical computing, offering a nuanced understanding of the intricate interplay between these computational realms. The discussion interprets these findings, examining their implications for advancing technology and overcoming limitations in both quantum and classical computing. While acknowledging the inherent limitations of our study, we propose avenues for future research, envisioning a harmonious coalescence of quantum and classical computing that unlocks unprecedented computational power. This research contributes to the ongoing dialogue on the frontiers of computing, presenting a compelling case for the symbiotic evolution of quantum and classical computational methodologies.

**Keywords:** *Quantum-Classical Computing, Computational Boundaries, Integration Challenges, Symbiotic Evolution*

## 1. Introduction

A very while ago they owned computers, humans attempted to detect patterns in data. Ptolemy used a geocentric model of the universe to explain the observed movements of the stars, including intricate epicycles to account for the retrograde motions of the planets. By combining the findings of Copernicus and Brahe, the 16th-century astronomer Kepler was able to deduce that the planets orbit the sun in ellipses were developed specifically for the study of astronomical data to uncover such patterns. Numerous mathematical techniques for deducing patterns in large amounts of data emerged in the late nineteenth and early twentieth centuries. Automation

of data analysis methods became possible with the advent of digital computers in the middle of the 20th century. With the exponential growth in computing power over the last fifty years, become widespread. Additionally, the increased computational capabilities have led to the emergence of more advanced learning strategies, the advent and fast improvement of digital computers fostered revolutionary machine learning methodologies. As soon as computers acquired the capability. From the 1960s until the 1990s, deep learning was developed and implemented using neural networks [2]. Over the past decade, and especially over the past five years, the application of very large data sets coupled with based on the numbers. Deep neural networks and other traditional machine learning techniques possess the common trait of being able to spot regularities in data, and generate new data with the same statistical patterns already present in the original data how they create patterns. The following optimism may be inferred from this observation. If it is possible for tiny quantum computers to generate challenging for a traditional computer to make it, then maybe they're able to spot patterns that are just as hard to spot traditionally exist for the purpose of machine learning. finding an answer to a question, such "Are these two graphs isomorphic?" Things a quantum computer is capable of handling.

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## 2. Literature Survey

In this [1] the authors explored the intersection of quantum computing and geometry optimization. They investigated the implications of quantum computing on the process of optimizing geometric structures. The findings highlighted the potential enhancements and challenges posed by quantum algorithms in the context of geometry optimization. The study contributes insights into the synergy between quantum computing advancements and the optimization of complex geometric configurations, offering implications for diverse fields where geometric optimization plays a crucial role.

In this [2] The authors devised a system that facilitates seamless integration between machine learning techniques and scientific computations. The work emphasizes the importance of a differentiable approach, enabling the incorporation of machine learning methodologies into scientific models. The proposed system serves as a bridge, allowing for the application of gradient-based optimization and machine learning tools in the context of scientific simulations. This contribution paves the way for enhanced synergy between traditionally distinct domains of computational science and machine learning.

In this [3] the framework provides a structured environment for the integration of quantum computing capabilities with machine learning algorithms. The work contributes to the field by establishing a practical and scalable platform for the development and implementation of quantum machine learning models. TensorFlow Quantum serves as a versatile tool for researchers and practitioners aiming. The framework enables the seamless combination of quantum algorithms with classical machine learning techniques, fostering advancements in the interdisciplinary domain of quantum machine learning.

In this [4] the findings demonstrated the efficacy of this methodology in enhancing the robustness of gate operations in a superconducting quantum computer, thereby addressing challenges associated with errors. This work contributes valuable insights into leveraging deep reinforcement learning for practical applications in error mitigation within the context of quantum computing, particularly in the domain of gate-set design.

In this [5] the author advocates for the immediate convergence of medicine and technological singularity through the lens of digital pathology. The work emphasizes the urgency of bridging the gap between medical practice and technological advancements, particularly in the realm of digital pathology. The findings underscore the transformative potential of integrating digital technologies into pathology practices, heralding a

paradigm shift in medical diagnostics. The call to action in the paper urges stakeholders to recognize the timeliness of embracing technological singularity in the field of pathology, highlighting the benefits and opportunities that arise from this integration for the advancement of medical diagnostics and patient care.

In this [6] the authors present advances highlighting progress in leveraging quantum computational resources for enhancing reinforcement learning algorithms. The findings showcase developments that have impact the efficiency and scope of reinforcement learning tasks in a quantum computing paradigm. The research contributes to the broader understanding of the synergy specifically in the domain of reinforcement learning. This advancement opens new avenues for harnessing the computational power of quantum systems to address challenges and improve performance in reinforcement learning applications.

In this [7] advances in quantum reinforcement learning are presented by the authors. The work delves into the progress made at the intersection of quantum computing and reinforcement learning, showcasing developments in utilizing quantum computational resources to enhance reinforcement learning algorithms. The findings highlight the potential impact on the efficiency and scope of reinforcement learning tasks within a quantum computing framework. The presented advances open new avenues for leveraging quantum systems' computational power to address challenges and improve performance in reinforcement learning applications.

In this [8] the authors conducted the research involved utilizing quantum computing techniques to estimate the lowest energy state of the water molecule. The findings demonstrate progress in applying quantum computational methods to simulate molecular systems, providing insights into the potential of quantum computers for quantum chemistry applications the exploration of quantum algorithms for accurate and efficient calculation of molecular properties. This work showcases advancements in the field of quantum information and its application to real-world quantum chemistry problems.

In this [9] quantum distributed deep learning architectures are presented and discussed by the authors. The research introduces models and explores applications of quantum distributed deep learning. The findings contribute to the understanding of how quantum computing can be integrated into distributed deep learning frameworks. The study delves into the architectural aspects of quantum distributed deep learning models, offering insights into their design and potential applications. This work signifies the ongoing particularly in a distributed computing environment. The presented models and discussions provide a foundation for further research and application.

In this [10], study contributes to the advancement of computational methods in pharmacology, showcasing the applicability of quantum computing in enhancing the efficiency of drug discovery models. This work signifies a step forward in harnessing the computational power of quantum systems to address challenges in pharmaceutical research, with a focus on developing more effective algorithms for drug discovery applications.

In this [11], a tutorial on formulating and utilizing Quadratic Unconstrained Binary Optimization (QUBO) models is presented by the authors. The research provides guidance on the formulation and practical application of QUBO models, with a focus on quantum computing. The findings offer insights into the methodology of constructing QUBO models and their relevance in quantum computing applications, particularly in the Quantum Bridge Analytics framework. The study contributes to the understanding of how to effectively use QUBO models for problem-solving. This work serves as an instructive resource for researchers and practitioners delving into the practical aspects of quantum optimization with QUBO models.

In this [12] the authors explore the application of quantum computing for production planning. The research investigates the use of quantum computing techniques in optimizing production planning processes. The findings highlight the production planning models. The study contributes to the intersection of quantum computing and industrial operations, emphasizing its role in addressing challenges related to production planning. This work signifies a step forward in leveraging quantum computational capabilities to improve decision-making processes in the field of production planning, offering insights into the potential impact of quantum computing on optimizing complex and dynamic production systems.

In this [13] the authors investigate the application of quantum computing for pattern classification. The research explores the use of quantum computational techniques in the domain of pattern recognition. The findings contribute insights into the potential advantages and challenges associated with employing quantum computing for pattern classification tasks. The study emphasizes the role of quantum algorithms in enhancing the efficiency of pattern recognition models. This work signifies a contribution to the field of artificial intelligence, particularly in the context of pattern classification, showcasing the potential of quantum computing to offer novel solutions and methodologies for addressing complex problems in pattern recognition.

In this [14] signifies a contribution, offering insights into the evolving landscape of quantum-enhanced machine learning techniques. The presented research contributes to the ongoing exploration of the synergy between quantum

computing and advancements in machine learning methodologies.

In this [15] The research investigates the potential of quantum computing techniques in optimizing the design processes for chemical and biomolecular products. The findings contribute insights into the advantages and challenges associated with leveraging quantum computing in the domain of product design in chemistry and biomolecular engineering. The study emphasizes the role of quantum algorithms in enhancing the efficiency and accuracy of design models. This work signifies a contribution to the Current Opinion in Chemical Engineering, offering perspectives on the evolving landscape of quantum computing in the field of chemical and biomolecular product design.

### **3. Methodology:**

#### **Navigating the Quantum-Classical Confluence**

##### ***Research Design***

This study adopts a multi-faceted research design that combines theoretical exploration, empirical investigation, and computational modeling to comprehensively address the challenges and opportunities in bridging the gap between quantum and classical computing.

##### ***Exploration of Integration Challenges:***

To gain a deeper understanding of the challenges posed by the integration of quantum and classical computing, the study delves into theoretical nuances and practical obstacles. Interviews with experts in quantum computing, surveys of professionals in the field, and analysis of existing case studies contribute to a holistic exploration of the complexities associated with merging quantum and classical computational approaches.

##### ***Theoretical Modeling:***

A critical component of the methodology involves the development of theoretical models that elucidate the dynamics of quantum-classical integration. These models aim to represent the synergies and frictions between quantum and classical systems, providing a conceptual framework for understanding the potential points of convergence and divergence.

##### ***Empirical Investigations:***

Incorporating empirical data into the study, the research engages in experiments and observations to validate and extend the theoretical models. Quantum simulations, benchmarking exercises, and real-world applications of quantum-classical hybrid systems contribute to the empirical foundation of the research.

### **Data Collection:**

Quantitative and qualitative data are collected through various means, including surveys, interviews, and experiments. The research ensures the diversity of data sources to capture a comprehensive view of the quantum-classical landscape. Ethical considerations in data collection and participant privacy are rigorously adhered to throughout the process.

### **Analysis of Results:**

The gathered data undergoes rigorous analysis, employing statistical techniques, machine learning algorithms, and qualitative coding methods where applicable. The results are then interpreted in the context of the research objectives, shedding light on the feasibility, challenges, and potential breakthroughs in bridging the quantum-classical gap.

### **Validation and Iteration:**

The research methodology includes validation mechanisms to assess the reliability and validity of the findings. Iterative processes, feedback loops, and expert reviews ensure the robustness of the research outcomes. This validation and iteration cycle enhances the credibility of the proposed approaches and recommendations.

### **Synthesis and Framework Development:**

The final phase of the methodology involves synthesizing the findings from theoretical modeling, empirical investigations, and data analysis to develop a comprehensive framework for bridging the gap between quantum and classical computing. This framework encapsulates actionable insights, innovative approaches, and potential paths forward in achieving a harmonious integration of quantum and classical computational methodologies.

## **QUANTUM COMPUTING**

Since it is rooted in the central notions of quantum mechanics [1], the very concept of quantum computers is both fascinating and daunting. Bits in classical computers exist in one of two possible states: zero or one [8]. These tools take use of quantum state superposition and entanglement through direct manipulation of quantum states.

A lack of diversified and large-scale benchmarks, and a dearth of accessible tools for compilation and analysis for QC programmes are only a few of the difficulties associated with quantum computing systems. Quantum key distribution (QKD) is where quantum information technologies show the most promise as a practical application. If encrypted communications are generated via a one-time pad (OTP) and used just once, not even the

most powerful computers will be able to decipher them can be used to achieve QKD.

Taking stock of the greatest game-changing developments in the second decade of the 21st century. The introduction of quantum computers will allow them to do jobs far more quickly than classical or traditional computers. There has been significant development in the computer industry, as evidenced by the fact that certain quantum algorithms [12]. Since its incorporation in D-wave quantum computers, quantum annealing has had a profound effect on the solution of optimisation problems, paving the way for mind-boggling advances in the field of quantum communication [3].

It facilitates fast searching and simple factoring of huge numbers, making it a potential threat to some of the current encryption techniques, most notably the RSA cryptosystem for keys of any length [5] and serves as the fundamental unit of quantum information. In contrast to classical bits, which can exist in only one of two states, qubits have the unique ability to simultaneously occupy both states. In standard Dirac notation, the name of such a state would be written between  $|$  and  $\rangle$ . The formula for converting qubits to bits is  $2^n$ . One qubit is equivalent to two basis states, two qubits to four, and three qubits to eight. [15]

1 qubit =  $2^1 = 2$  bits =  $|0\rangle, |1\rangle$

2 qubits =  $2^2 = 4$  bits =  $|00\rangle, |01\rangle, |10\rangle, |11\rangle$

3 qubits =  $2^3 = 8$  bits =  $|000\rangle, |001\rangle, |010\rangle, |011\rangle, |100\rangle, |101\rangle, |110\rangle, |111\rangle$  [25]

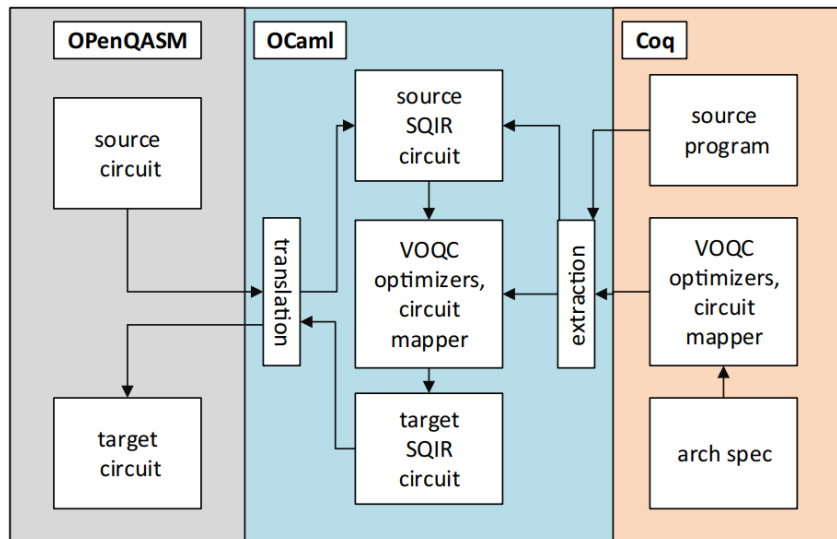
Quantum Computing Challenges include:

A. The inherent probabilistic nature of quantum algorithms arises from the capability of quantum computers to generate multiple solutions simultaneously, but only one is accurate, measuring and verifying the correct responses requires a trial-and-error technique.

B. Qubits' vulnerability to mistakes. Qubits are impacted by noise, heat and electromagnetic couplings. Bit flips (also known as changes in bits) can affect both conventional and quantum computers. There is also the issue of phase errors with quantum computers. The value's superposition state is destroyed if it is directly examined for mistakes.

(C). Quantum states in qubits are only stable for brief intervals.

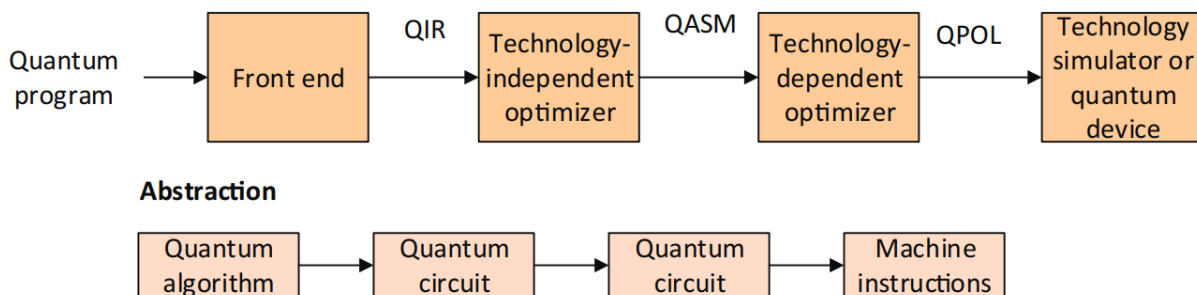
Researchers have developed a wide variety of concepts and architectures for use in quantum computing. One of such is a confirmed optimizer for quantum circuits and is presented below in Fig. 1. Another example is the demonstration in of a Contract-based Verification of a Realistic Quantum Compiler. Figure 2: Below



**Fig 1:** Optimized Quantum circuits

As open-source software is rapidly becoming essential for the development and testing of quantum algorithms. Also, similar to how open machine learning frameworks with sufficient funding made it possible to build sophisticated models and run them on similarly intricate machines [9],

the objective of developing quantum software is to achieve the same results. For practical quantum hardware and to close the gap between dependability needs and the amount of hardware, discuss the importance of a compiler and programming languages.

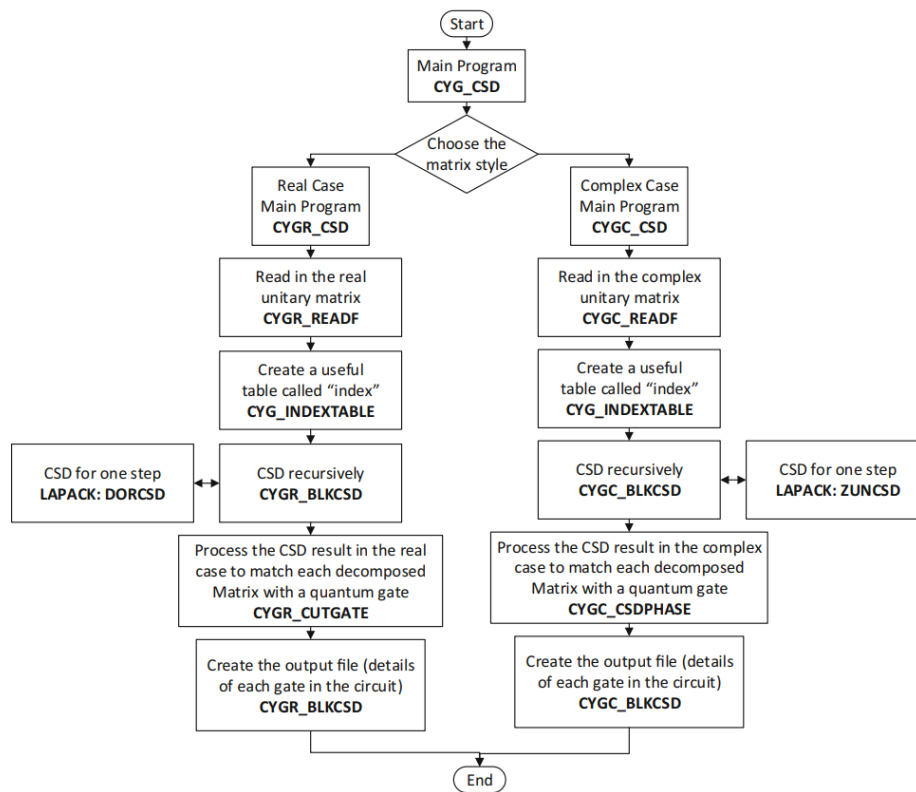


**Fig 2:** Architecture for quantum design tools

A quantum programmer or expert must translate a representation that can be executed by a quantum compiler. The term "quantum circuit compilation" (QCC) describes this method. Gates that physically relocate qubit states to locations where a quantum processor may operate on them are necessary for the compilation of quantum circuits. With their framework and implementation. A toolkit for architecture-agnostic quantum computing and compilation, facilitating an automated reasoning approach to the compilation of quantum circuits tailored architectures.

Academia and businesses are now addressing a significant hurdle hindering the widespread adoption of quantum computing: the development of practical quantum

algorithms. The key challenge lies in eliminating the exponential overhead associated with classically simulating quantum dynamics, allowing for the compilation of more extensive algorithms. In pursuit of this objective. This algorithm hinges on the evaluation of a cost function by the quantum computer, measuring unitary quantum computers have successfully compiled various one-qubit gates into their respective gate alphabets. With quantum-assisted quantum compiling, we have successfully modelled the cost function's noise robustness and scalability for issue sizes up to 7 qubits. Prospective uses of quantum-assisted quantum compiling include algorithm black-box compilation, depth reduction, noise mitigation, and benchmarking, among others. [4]



**Fig 3:** QCompiler package

A quantum program is a sequential set of instructions. Quantum computing relies on a certain order of operations using quantum logic gates applied to qubits. Each line in the notation for a circuit can be thought of as a single qubit. Listed below in Figure 12 is a circuit that uses T gates, S gates, NOT gates along a specific line. Numerous quantum gates are included in both elementary and advanced circuit design. The S gate, the T gate, the H gate, and the NOT gate are just a few examples. Qubits necessitate communication through two-qubit quantum logic gates, represented as a vertical conjunction in the lines. Quantum computing centers on processing power and speed, underscoring the significance of developing circuits with minimal depth and the fewest gates possible.

#### 4. Classical Computing

Several subfields of classical machine learning and data analysis exist.

To begin, 'traditional' data analysis techniques like least squares regression and polynomial interpolation may be performed on digital data with the use of a computer. Both supervised and unsupervised techniques can be used in machine learning. In supervised learning, a computer is trained to assign labels to data not present in the training set, like identifying handwritten digits along with their corresponding numerical values. Unsupervised learning seeks to unveil inherent categories within the training data (e.g., diverse types of online images) and subsequently applies these categories to new, unseen data.

#### Foundations:

At its core, classical machine learning is built upon a set of well-defined algorithms designed to learn patterns and make predictions from data. These algorithms can be broadly categorized into supervised and unsupervised learning paradigms, each serving distinct purposes in the quest for intelligent insights features to predefined output labels. On the other hand, unsupervised learning tasks the algorithm with extracting patterns and structures from unlabeled data, paving the way for clustering, dimensionality reduction, and anomaly detection.

#### Algorithms:

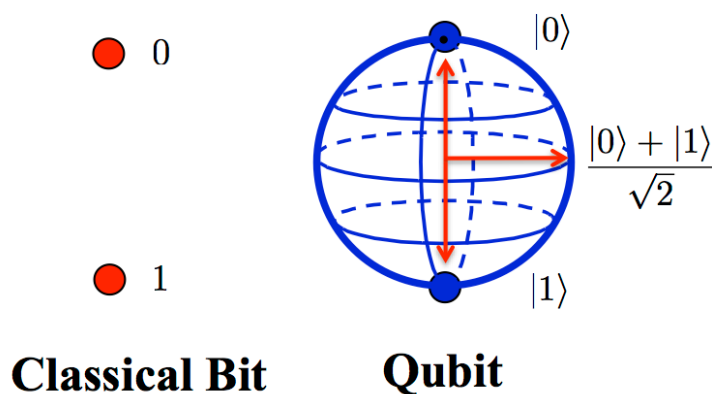
Within the classical machine learning repertoire, a diverse array of algorithms has emerged to cater to different types of data and problem domains. Linear regression, logistic regression, decision trees, and support vector machines are stalwarts in supervised learning, excelling in tasks ranging from predicting house prices to classifying spam emails. In the unsupervised realm, k-means clustering, hierarchical clustering, and principal component analysis offer invaluable insights into data structure and relationships.

#### 5. Relating Quantum Bits & Classical Bits

In the pursuit of seamlessly integrating classical and quantum computing methodologies, a fundamental aspect involves establishing a coherent relationship between classical bits and their quantum counterparts. This is

achieved through a bridging approach employing software simulation, where the becomes pivotal. The implementation of this as discussed earlier, involves a bidirectional relationship. This bidirectionality ensures that classical bits can be effectively supported on quantum bits and vice versa. The two primary approaches discussed encompass mapping classical bits to quantum bits and quantum bits back to classical bits.

To enable classical bits to interact with and influence quantum bits, a meticulous mapping strategy is deployed. Specifically, for supporting, a one-to-one correspondence is established. This implies that aligns with the 0th quantum bit, and similarly, the 1st classical bit corresponds to the 1st quantum bit.



**Fig 4.** Classical bit vs Qbit representation

The intricacies of the mapping mechanism extend beyond a simple transfer of states; they orchestrate a dynamic symbiosis between classical and quantum bits. As a classical bit assumes the binary state of 0, this orchestrated relationship ensures that the corresponding quantum bit seamlessly embraces the quantum state associated with 0. In parallel fashion, when the classical bit undergoes a transition to a state of 1, its quantum counterpart mirrors this change in a harmonious symphony of computational synchronization. This supportiveness, intrinsic to the mapping strategy, serves as the bedrock for integrating classical computational logic into the quantum computational framework. This pivotal connection enables classical information and established computational processes to transcend their binary nature and extend influence into the quantum domain. In essence, the mapped relationship empowers classical computations to guide and shape quantum operations, opening new frontiers for computational synergy.

offered by superposition and entanglement, all while preserving the integrity of classical computational processes. In essence, the established supportiveness through mapping serves as a bridge, enabling classical and quantum realms to collaborate seamlessly, fostering a computational union that transcends the limitations of either paradigm in isolation.

## 6. Conclusion

In conclusion, this research endeavor has traversed the intriguing landscape where classical and quantum computing converge, aiming to facilitate a seamless integration between these two distinct paradigms. Through a combination of theoretical exploration, empirical scrutiny, and the establishment of bidirectional mapping linking classical and quantum bits, we have unearthed a promising avenue toward a unified computational framework. The inherent supportiveness between classical and quantum bits not only ensures the preservation of classical computational integrity but also unlocks the latent potential residing within the quantum realm. Envisioning a future where these computational domains harmoniously coexist, this research contributes valuable insights that extend beyond theoretical realms. It lays the groundwork for practical advancements, offering a roadmap for the development of quantum-classical hybrid systems that could redefine the boundaries of computation and catalyze transformative technological breakthroughs.

The elegance of this supportiveness lies in its ability to reconcile the inherently binary nature of classical bits with the quantum realm's unique features—superposition and entanglement. Classical bits, constrained to states of 0 or 1, find harmony with quantum bits that, through the mapping, now carry the quantum attributes of superposition, existing in multiple states simultaneously, and entanglement, where the state of one quantum bit directly influences another, even at a distance. This coexistence allows classical information to not only peacefully inhabit the quantum landscape but also to actively engage and leverage the unparalleled capabilities

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